Introduction to X-ray Absorption Spectroscopy

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XAS 2023: Fundamentals of XAS Data Analysis: A Hands-on Tutorial 10 October, 2023 Part 1

The basic physics and chemistry of X-ray Absorption

This Talk

This talk is an introduction to the inner-shell spectroscopies, XAS and XRF.

Outline

- An overview of the basic physics of inner shell spectroscopies
- An introduction to XAS and XRF beamline instrumentation
- A flavor of the sorts of science that can be accomplished with XAS and XRF, including examples from my own research and my beamline.

My hope is that you will leave with a sense of how XAS and XRF might be applied to your research.

XAS and XRF

X-ray Absorption Spectroscopy and X-Ray Fluorescence spectroscopy

These are inner shell spectroscopies.

Inner shell means that an x-ray interacts primarily with a deep-core electron rather than with a valence

Spectroscopy means that some aspect of the interaction changes as a function of photon energy.

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XAS and XRF

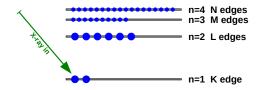
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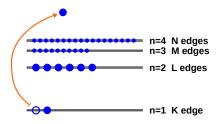
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-rays and electrons XAS XRF XAS measurement Vocabulary



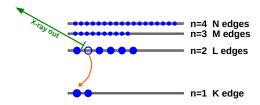
- An incoming photon interacts with a deep-core electron. Shown here, a 1s electron is excited for a K-edge spectrum.
- The deep-core electron is promoted to some unoccupied state above the Fermi energy, propagates away, and leaves behind a core-hole.
- A short time later (1 or 2 femtoseconds), a higher-lying electron decays into the core-hole and emits a photon. Shown here, a 2p^{3/2} or 2p^{1/2} electron fills the 1s hole
- Alternately, the energy from the higher-lying electron can be used to emit an Auger electron.

-rays and electrons XAS XRF XAS measurement Vocabulary



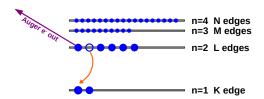
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rays and electrons XAS XRF XAS measurement Vocabular



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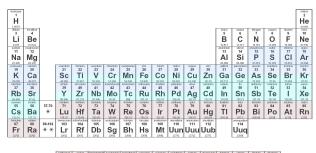
rays and electrons XAS XRF XAS measurement Vocabu



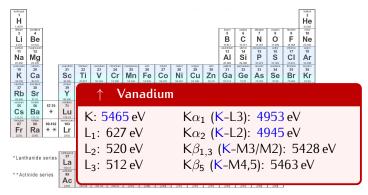
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XAS XRF XAS measurement

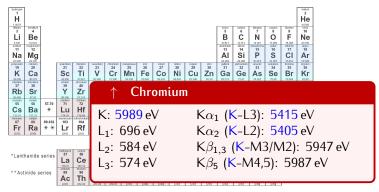
Elements and Beamlines



Elements and Beamlines

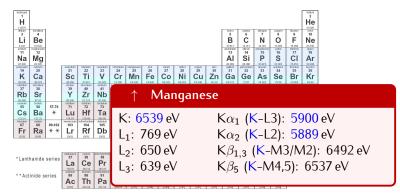


Elements and Beamlines

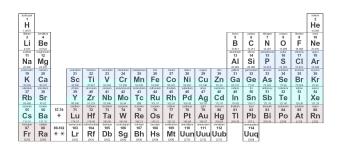


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Elements and Beamlines



Elements and Beamlines



*Lanthanide series

Če Pr Ac Th Pa * * Actinide series

Nd Pm Sm Eu Gd Tb Dy Ho Er Tm Yb

Uranium

K- or L-edges me K-edges measu

L-edges measu

K: 115606 eV $L\alpha_1$ (L3-M5), 13614 eV L₁: 21757 eV $L\alpha_2$ (L3-M4), 13438 eV L₂: 20948 eV $L\beta_2$ (L3-N4,5), 16388 eV

L₃: 17166 eV $L\beta_5$ (L3-O4,5), 17063 eV

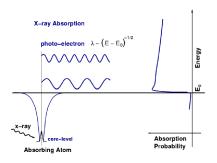
 $L\beta_6$ (L3-N1): 15727 eV

L_ℓ (L3-M1): 11618 eV

K-rays and electrons XAS XRF XAS measurement Vocabulary

A simple picture of X-ray absorption

An incident x-ray of energy E is absorbed, destroying a core electron of binding energy E_0 and emitting a photo-electron with kinetic energy $(E-E_0)$. The core state is eventually filled, ejecting a fluorescent x-ray or an Auger electron.



An empty final state is required.

No available state,

no absorption!

When the incident x-ray energy is larger than the binding energy,

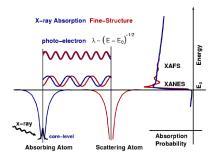
there is a sharp increase in absorption.

For an isolated atom, $\mu(E)$ has a sharp step at the core-level binding energy and is a smooth function of energy above the edge.

X-rays and electrons $egin{pmatrix} XAS \end{pmatrix}$ XRF XAS measurement Vocabulary

X-ray absorption in condensed matter

The ejected photo-electron can scatter from neighboring atoms. R has some relationship to λ and there is a phase shift associated with the scattering event. Thus the outgoing and scattered waves interfere.

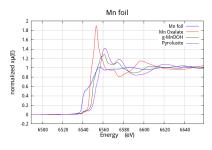


The scattering of the photo-electron wave function interferes with itself.

 $\mu(E)$ depends on the density of states with energy $(E-E_0)$ at the absorbing atom.

This interference at the absorbing atom will vary with energy, causing the oscillations in $\mu(E)$.

XAS and Valence State

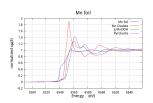


As the valence increases $Mn^0 \rightarrow Mn^{2+} \rightarrow Mn^{3+} \rightarrow Mn^{4+}$ the edge position shifts to higher energy.

XAS is a direct measure of valence state

- Since each element has its own edge energy, an element's valence can be measured even in a heterogeneous sample
- Since x-rays are deeply penetrating into matter, samples often require only preparation
- No assumption of symmetry or periodicity is made, so the sample can be crystalline, amorphous, thin film, in solution, surface sorbed, \cdots , whatever

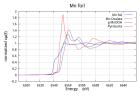
XAS and Local Atomic Structure

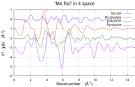


- The different Mn species display big differences in the fine structure beyond the edge as the valence increases (Mn⁰, Mn²⁺, Mn³⁺, Mn⁴⁺). The white line and subsequent oscillations are quite different.
- The oscillatory portion of the spectrum can be isolated and

... Fourier transformed. This FT function can be interpreted to yield partial pair distribution functions of atoms about the absorber. The Mn-O distances are different for the Mn²⁺, Mn³⁺, and Mn⁴⁺ and clearly different from the Mn-Mn distance in Mn metal.

XAS and Local Atomic Structure

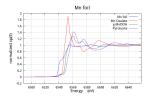


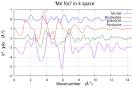


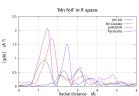
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K-rays and electrons $egin{pmatrix} XAS \end{pmatrix}$ XRF XAS measurement Vocabulary

XAS and Local Atomic Structure







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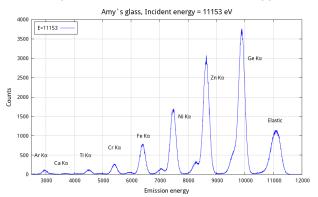
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Fluorescence from Many Elements

X-ray fluorescence is a spectroscopy in which the incident energy is fixed and the energy dependence of the secondary photons is measured.

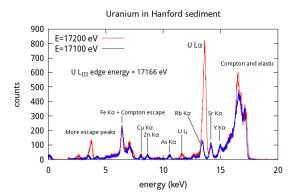
Every element with an edge below the incident energy will fluoresce.

Glass with every 2^{nd} element Ca–Ge, incident energy = $11153 \, eV$



Fluorescence from A Sediment Sample

Here are the XRF spectra with incident beams above and below the U L_{III} edge for a sediment heavily contaminated with uranium.

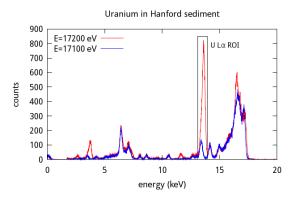


When combined with a standard measured under identical conditions, element concentrations can be *quantified*.

Grays and electrons XAS XRF XAS measurement Vocabulary

Using the Fluorescence Spectrum for XAS

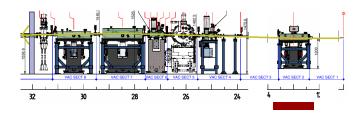
We can place a region of interest (ROI) around the U L α peak and measure its variation as a function of incident energy.



In this way, we measure signal only from the absorber and reject all other photons entering the detector.

K-rays and electrons XAS XRF XAS measurement Vocabulary

Typical optics for an XAS beamline



Collimating mirror

Makes the divergent rays from the source parallel, setting the beam size $(8 \text{ mm} \times 1 \text{ mm} \text{ at BMM})$



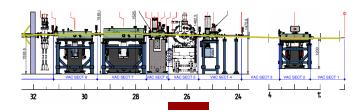
Total external reflection from a paraboloid surface



All instrumentation images are from FMB Oxford Beamlines Ltd.

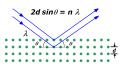
X-rays and electrons XAS XRF (XAS measurement) Vocabulary

Typical optics for an XAS beamline



Monochromator

Bragg diffraction from a Si crystal to pass a narrow bandwidth from the pink beam



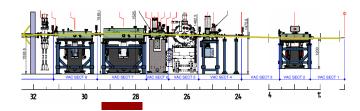
Change energy by changing angle



All instrumentation images are from FMB Oxford Beamlines Ltd.

X-rays and electrons XAS XRF (XAS measurement) Vocabulary

Typical optics for an XAS beamline



Focusing mirror

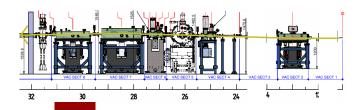
Total external reflection from a torroid surface, bent such that rays focus to a spot





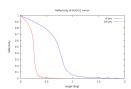
All instrumentation images are from FMB Oxford Beamlines Ltd. Photo of mirror is from ESRF ID09B X-rays and electrons XAS XRF XAS measurement Vocabulary

Typical optics for an XAS beamline



Harmonic rejection mirror

Flat mirror redirects beam from mono and M2



Choose an angle to pass the fundamental but absorb harmonics



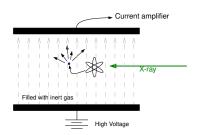
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K-rays and electrons XAS XRF XAS measurement Vocabulary

A typical XAS hutch (BMM at NSLS-II)



Ionization chambers

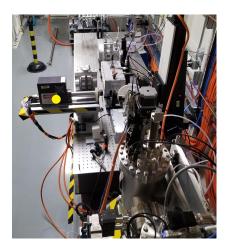


Gas-filled capacitors. Incoming photon ionizes a gas molecule. The electron cascade produces a measurable current.

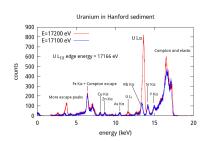
Transmission XAS
$$\mu(E) = \ln(I_0/I_t)$$
i.e. Beers' Law for X-rays

Grays and electrons XAS XRF $\overline{ ext{XAS measurement}}$ Vocabulary

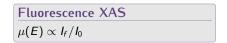
A typical XAS hutch (BMM at NSLS-II)



Energy discriminating fluorescence detector

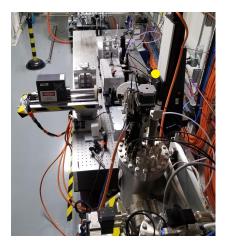


Silicon drift diode measures energy of each photon deposited



K-rays and electrons XAS XRF (XAS) measurement Vocabulary

A typical XAS hutch (BMM at NSLS-II)



Sample stage

Hard X-rays are deeply penetrating into matter, so the stage could be:

- Cryostat
- Furnace
- Pressure cell
- Electrochemistry cell
- Stop-flow cell
- Gas flow reactor
- Controlled atmosphere

etc. etc. etc.

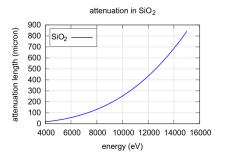
Real samples under real conditions

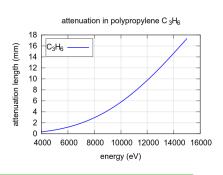
-rays and electrons XAS XRF (XAS measurement) Vocabulary

What is meant by "deeply penetrating"?

The Center for X-ray Optics provides a tool for estimating the attenuation of X-rays as they pass through matter.

http://henke.lbl.gov/optical_constants/atten2.html





So, windows made of low-Z materials can be quite thick and still pass hard X-rays. This allows deployment of specialized sample environments for use in XAS experiments.

-rays and electrons XAS XRF XAS measurement (Vocabulary)

Acronyms

XANES X-ray Absorption Near-Edge Structure
NEXAFS Near-Edge X-ray Absorption Fine Structure

XANES and NEXAFS are <u>exactly</u> the same thing. Historically, the soft X-ray community says "NEXAFS" while the hard X-ray community says "XANES".

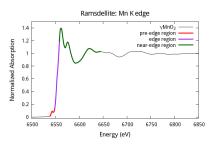
Both acronyms refer to the portion of the XAS (X-ray Absorption Spectroscopy) measurement in the vicinity of the absorption edge.

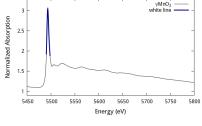
The Extended X-ray Absorption Fine Structure is oscillatory data extending hundreds of volts above the edge.

-rays and electrons XAS XRF XAS measurement (Vocabulary)

Some vocabulary

Words commonly used to describe specific parts of the XANES spectrum.





LaTiO2N: La LIII edge

pre-edge Small (or large, certainly meaningful!) features between the Fermi energy and the threshold

edge The main rising part of XAS spectrum

near-edge Characteristic features above the edge

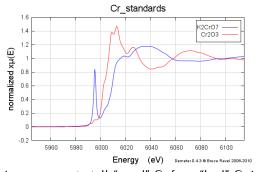
white line Large, prominent peak just above the edge, particularly in L or M edge spectra

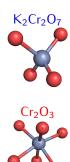
Part 2

Understanding XANES

Speciation at a glance: Coordination

Here is Cr K edge data for tetragonally coordinated, hexavalent $K_2C_2r^{VI}O_7$ and hexagonally coordinated, trivalent $Cr_2^{III}O_3$. Trivalent Cr is insoluble and non-toxic. Hexavalent Cr is readily soluble and highly toxic.



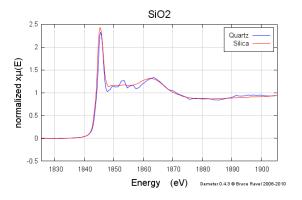




It is very easy to tell "good" Cr from "bad" Cr in a XANES measurement.

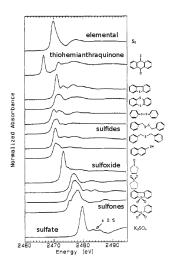
Speciation at a glance: Crystallinity

 SiO_2 is found in two forms* under standard conditions: crystalline (the mineral quartz) and amorphous (common glass).



Again, these are readily distinguished by a XANES measurement.

Speciation at a glance: Oxidation



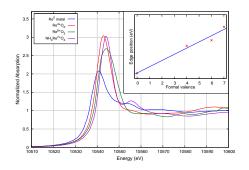
- There is an 11 eV shift from S^{2-} to S^{6+} with lots of variation among species.
- S speciation is of importance across a broad range of disciplines, including life science, catalysis, petroleum science, photovoltaics, environmental science and more.
- P and Cl are similarly rich in their XAS.

Sulfur K-edge x-ray absorption spectroscopy of petroleum asphaltenes and model compounds, G.N. George, M.L. Gorbaty, J. Am. Chem. Soc. (1989) 111:9, 3182 *B DOI: 10.1021/ja00191a012

Oxidation and edge position

There is a relationship between formal valence of a metal and the position of the edge in the XANES spectrum. Here is Re metal along with 4+, 6+, and 7+ oxides of Re.

The shift to higher energy is, to first order, a Coulomb effect. Less charge on the atom means less screening of the core.



Some more examples:

Mo S.P. Cramer et al. J. Am. Chem. Soc., **98**:5, pp 1287 (1976)

₾ DOI: 10.1021/ja00421a053

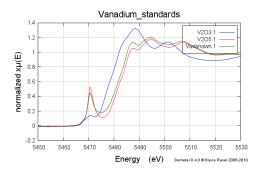
V J. Wong et al. Phys. Rev. B30, 5596–5610 (1984) № DOI: 10.1103/PhysRevB.30.5596

Simultaneous XAFS measurements of multiple samples, B. Ravel, C. Scorzato, D.P. Siddons, S.D. Kelly and S.R. Bare, J. Synchrotron Rad. (2010) 17, 380-385

¹a DOI: 10.1107/S0909049510006230

Mixed phases

Here we see trivalent V_2O_3 , pentavalent V_2O_5 and an unknown Vanadium compound plotted together.



Like in the Cr example, we see a distinct difference between 6-coordinated and 4-coordinated V.

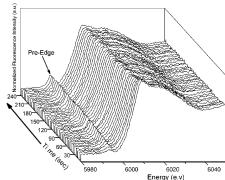
Our unknown is partially reduced, as can be seen by the reduction in pre-edge peak and the left-ward shift of the main edge.

Later we will discuss ways of determining the content of the unknown.

Evolution of redox state

The edge features are often large enough that their evolution can be measured in an *in situ* experiment.

Here we see the kinetics of $Cr^{III} \rightarrow Cr^{VI}$ oxidation by Mn oxide over the course of four minutes of reaction time. Each scan was measured in 3 second.

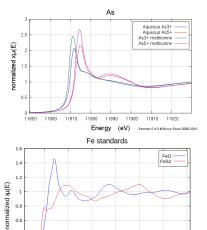


The *in situ* experiment could involve a chemical reaction, a change in temperature, electrochemical cycling, and so on.

Kinetics of Chromium(III) Oxidation by Manganese(IV) Oxides Using Quick Scanning X-ray Absorption Fine Structure Spectroscopy (Q-XAFS), G. Landrot, M. Ginder-Vogel, and D.L. Sparks, Environ. Sci. Technol., (2010) 44:1, pp 143-149

30 DOI: 10.1071/ex901750w

Ligands



Energy (eV)

7220 7240

0.4

0.2

7120 7140

We see a significant edge shift between aqueous As³⁺ and aqueous As⁵⁺, as we expect. Note that the As³⁺ and As⁵⁺ methionine solutions are similar, but shifted to lower energy.

The same shift is seen between divalent wüstite (FeO) and divalent pyrite (FeS₂).

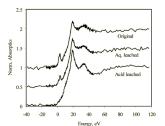
Fingerprinting

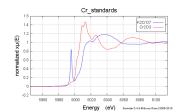
Fingerprint, tr.v.

To identify by means of a distinctive mark or characteristic.

One of the most powerful uses of XANES data is to simply identify what is in front of the beam.

Looking back at the Cr^{III}/Cr^{VI} example, what might you say about the valence of the chromium contained in coal combustion residue?





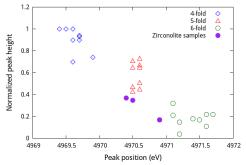




Quantifying Hazardous Species in Particulate Matter Derived from Fossil-Fuel Combustion, F.E. Huggins, et al., Environ. Sci. Technol. (2004) 38:6, 1836 & DOI: 10.1021/es0348748

Categorizing spectra

In an study of Ti-containing standard materials, the different coordination environments were found to aggregate when plotting pre-edge peak height v. peak position.



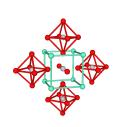
Here we see the data from the reference below along with Ti K-edge data from various Zirconolite $(CaZrTi_2O_7)$ samples.

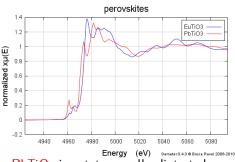
F. Farges, G.E. Brown Jr., J.J. Rehr, Coordination chemistry of Ti (IV) in silicate glasses and melts: J. XAFS study of titanium coordination in axide model compounds, Geochim. Cosmochim/ Acta, 60:16, 3023, 1996, *a DOI: 10.1016/0016-7037/96/00144-5

Α

XANES and disorder

The details of the XANES can often give information about structural disorder about the absorbing atom.





EuTiO₃ is a true cubic perovskite. PbTiO₃ is a tetragonally distorted perovskite with substantial disorder in the oxygen octahedron. Consequently, the pre-edge peak is much larger for PbTiO₃.

B. Ravel, E. A. Stern, R. I. Vedrinskii, V. Kraizman, Local structure and the phase transitions of BaTiO₂ Ferroelectrics, 206:1 (1998) 407,

Why are local disorder and the pre-edge peak related?

- For a K-edge spectrum, the initial state is s: $\ell=0$. Thus the final state must be $\ell=1$.
- ullet Ti has a filled p shell but a completely empty d shell.
- With centro-symmetry, as in a true perovskite, the p and d states cannot hybridize. Broken symmetry leads to mixing of p and d states around the Fermi level.
- Disorder-driven admixture of d character results in an enhanced pre-edge peak.

Analysis

There are a number of ways to get quantitative results from XANES spectra. Here's an incomplete list:

Linear Combination Fitting

Interpret data by comparison with standards

Peak Fitting

Fit peak-like and step-like line-shapes to the XANES data

Principle Components Analysis

Decompose an ensemble of data into a mathematical basis

Difference Spectra

Subtract one normalized spectrum from another

LCF

The working assumption of LCF

The spectrum from an unknown sample can be understood as a linear superposition of the spectra of two or more known samples.

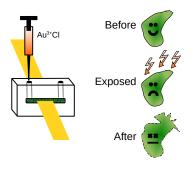
That is:



XANES Information XANES Fingerprinting (XANES Analysis)

Economic geology (I)

One way that gold deposits form is by having Au chloride fluids rise from the deep earth, wash over cyanobacteria colonies, and reduce to metallic gold.



We simulated this process at the beamline by exposing cyanobacteria to an Au^{3+} solution and "watching" the evolution of the $Au\ XAS$ from Au^{3+} to Au^0 .

Questions

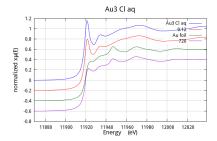
- What is the rate constant?
- Is there an intermediate species?

M. Lengke et el., Mechanisms of Gold Bioaccumulation by Filamentous Cyanobacteria from Gold(III)-Chloride Complex, Environ. Sci. Technol. 40(20) p. 6304-6309. (2006) a DOI: 10.1021/es061040r

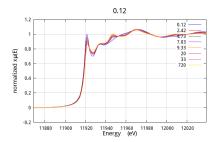
XANES Information XANES Fingerprinting (XANES Analysis)

Economic geology (II)

We see that 7 minutes after injection, the data strongly resemble the $Au^{3+}Cl$. After one week, the data resemble Au metal.



Over the course of the time series, the white line ~ 11921 shrinks while the bump ~ 11945 grows, suggesting the reduction to Au metal.

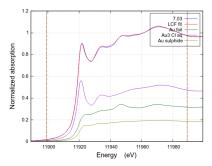


M. Lengke et el., Mechanisms of Gold Bioaccumulation by Filamentous Cyanobacteria from Gold(III)-Chloride Complex, Environ. Sci. Technol. 40(20) p. 6304-6309. (2006) a DOI: 10.1021/es061040r

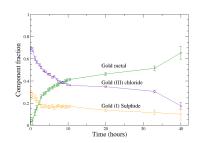
XANES Information XANES Fingerprinting (XANES Analysis)

Economic geology (III)

We can analyze these data as a linear combination of species, including $Au^{3+}Cl$, Au metal, and Au^{1+} sulfide.



We can plot out the contributions from these species as a function of time to get a sense of reaction rates.



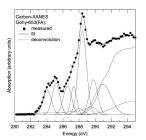
M. Lengke et el., Mechanisms of Gold Bioaccumulation by Filamentous Cyanobacteria from Gold(III)-Chloride Complex, Environ. Sci. Technol. 40(20) p. 6304-6309. (2006) a DOI: 10.1021/es061040r

XANES Information XANES Fingerprinting XANES Analysis

Peak fitting

The working assumption of peak fitting

A spectrum can be meaningfully deconstructed into a set of step-like (atan or erfc) and peak (Gaussian, Lorentzian, Voight) functions.



In this case, various Gaussians are interpreted as the main $1s-\pi^*$ or Rydberg/mixed valence transitions and two higher energy $(1s-2\pi^*)$ transition in the C K-edge XANES of a sediment.

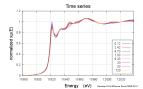
This sort of analysis is most meaningful when performed across an ensemble of related data. The drawback is that the physical significance of the line-shapes is sketchy, at best.

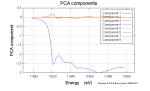
T. Schäfer, et al., Organic Geochemistry, 36:4, (2005) 567, a DOI: 10.1016/j.orggeochem.2004.10.011 Introduction to X-ray Absorption Spectroscopy

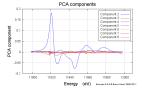
XANES Information XANES Fingerprinting (XANES Anallysis)

XANES: Principle Components Analysis

PCA is a bit of linear algebra which breaks down an ensemble of related data into abstract components.







The components can then be used to try to construct a standard as a test to see whether that standard is present in the ensemble.

The number of species represented in the ensemble is related to the number of statistically significant components.





S.R. Wasserman, J. Phys. IV France (1997) C2-203-C2-205; a DOI: 10.1051/jp4/1997163
S.R. Wasserman et al., J. Synchrotron Rad. (1999) 6, 284-286; a DOI: 10.1107/S0909049599000965

+ references therein

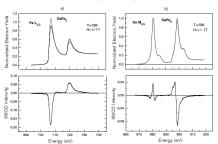
+ references theret

Difference Spectra

Difference spectra

Subtract one spectrum from another.

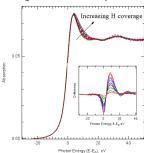
The most common use is for X-ray Magnetic Circular Dichroism (XMCD)



The areas under the difference spectra tell you about moment and magnetic ordering.

X-ray magnetic circular dichroism study on CeFe2, A. Delobbe, et al., Europhys. Lett. 43 320 (1998), a DOI: 10.1209/epl/i1998-00359-2 Pt data courtesy of Simon Bare

Difference spectra can also be used to highlight a subtle change in a data sequence.



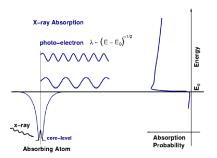
Here, hydogenation of the Pt nanoparticles alters the Pt DOS

Part 3

Understanding EXAFS

A simple picture of X-ray absorption

An incident x-ray of energy E is absorbed, destroying a core electron of binding energy E_0 and emitting a photo-electron with kinetic energy $(E - E_0)$. The core state is eventually filled, ejecting a fluorescent x-ray or an Auger electron.



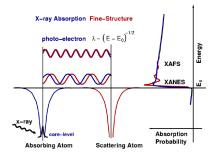
An empty final state is required. No available state. no absorption! When the incident x-ray energy is larger than the binding energy,

> there is a sharp increase in absorption.

For an isolated atom, $\mu(E)$ has a sharp step at the core-level binding energy and is a smooth function of energy above the edge.

X-ray absorption in condensed matter

The ejected photo-electron can scatter from neighboring atoms. R has some relationship to λ and there is a phase shift associated with the scattering event. Thus the outgoing and scattered waves interfere.



The scattering of the photo-electron wave function interferes with itself.

 $\mu(E)$ depends on the density of states with energy $(E-E_0)$ at the absorbing atom.

This interference at the absorbing atom will vary with energy, causing the oscillations in $\mu(E)$.

The EXAFS equation

For each kind of path, we evaluate the EXAFS equation:

$$\chi(k,\Gamma) = \frac{(N_{\Gamma}S_0^2)F_{\Gamma}(k)e^{-2\sigma_{\Gamma}^2k^2}e^{-2R_{\Gamma}/\lambda(k)}}{2kR_{\Gamma}^2}\sin\left(2kR_{\Gamma} + \Phi_{\Gamma}(k)\right) \tag{1}$$

$$\chi_{\text{theory}}(k) = \sum_{\Gamma} \chi(k, \Gamma) \tag{2}$$

$$R_{\Gamma} = R_{0,\Gamma} + \Delta R_{\Gamma} \tag{3}$$

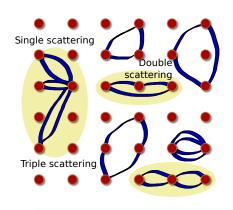
$$k = \sqrt{2m_e(E_0 - \Delta E_0)/\hbar^2} \approx \sqrt{(E_0 - \Delta E_0)/3.81}$$
 (4)

The terms in blue come from theory. (I use a thing called FEFF). FEFF treats SS and MS paths **equivalently**. F_{Γ} and ϕ_{Γ} are the *effective* scattering amplitude and phase shift for the path.

The strategy of EXAFS analysis

In IFEFFIT the terms in red are not themselves the fitting parameters. They are written in terms of the actual fitting parameters.

Real space multiple scattering in pictures



Here are some examples (in two dimensions) of single, double, and triple scattering paths.

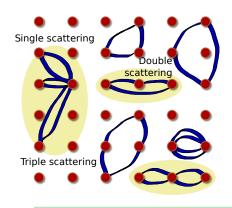
For SS, FEFF computes the three SS paths shown and all others (up to some maximum length).

SS and *collinear* MS paths tend to be the dominant contributions to the EXAFS.

The trick to EXAFS analysis

Somehow evaluate each path and choose which ones to include in a fit

Real space multiple scattering in pictures



Here are some examples (in two dimensions) of single, double, and triple scattering paths.

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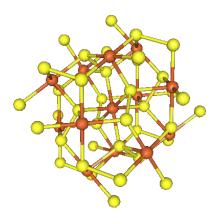
Somehow evaluate each path and choose which ones to include in a fit.

How we understand EXAFS

An example: FeS₂

More examples

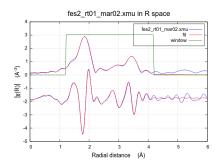
FeS₂ structure



Somehow add up the contributions from each of the scatterers and from all the MS paths involving those scatterers.

The Fe atom is surrounded by an octahedron of S atoms

- 6 S nearest neighbors at 2.257 Å
- 6 S next nearest neighbors at 3.445 Å
- 2 S scatterers at 3.594 Å
- 12 Fe scatterers at 4.167 Å



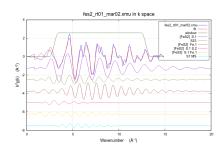
Path expansion

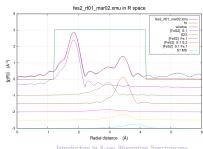
$$\chi(k,\Gamma) = \frac{(N_{\Gamma}S_0^2)F_{\Gamma}(k)e^{-2\sigma_{\Gamma}^2k^2}e^{-2R_{\Gamma}/\lambda(k)}}{2kR_{\Gamma}^2}\sin(2kR_{\Gamma} + \Phi_{\Gamma}(k))$$
(1)
$$\chi_{\text{theory}}(k) = \sum_{\Gamma}\chi(k,\Gamma)$$
(2)

$$\chi_{\text{theory}}(k) = \sum_{\Gamma} \chi(k, \Gamma)$$
(2)

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$$k = \sqrt{2m_e(E_0 - \Delta E_0)/\hbar^2} \approx \sqrt{(E_0 - \Delta E_0)/3.81}$$
 (4)





 \blacksquare

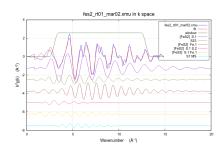
Path expansion

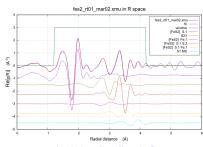
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$$k = \sqrt{2m_e(E_0 - \Delta E_0)/\hbar^2} \approx \sqrt{(E_0 - \Delta E_0)/3.81}$$
 (4)





 \blacksquare

Minerology (I)

A deep understanding of the nuclear fuel cycle requires study of "exotic" pentavalent uranium minerals that can form under specific mine or storage facility conditions. One such mineral, $U^{V}(H_{2}O)_{2}(U^{VI}O_{2})_{2}O_{4}(OH)+4\cdot H_{2}O, \text{ has recently been synthesized.}$

20/2(0 02/204(01)) 11/20, indirecting been

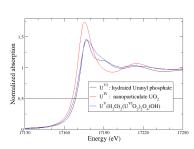
XRD is an indirect measure of valence — XAS is a direct measure!

N. Belai et el., *Pentavalent Uranium Oxide via Reduction of* [UO₂]²⁺ *Under Hydrothermal Reaction Conditions*, Inorg. Chem., 2008, 47 (21), pp 10135-10140, a DOI: 10.1021/ic801534m

Minerology (II)

XAS on $U^{V}(H_{2}O)_{2}(U^{VI}O_{2})_{2}O_{4}(OH)+4\cdot H_{2}O$

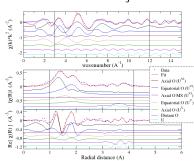
XANES data



We see evidence of U^V by the intermediate edge position between our U^{IV} and U^{VI} standards.

N. Belai et el., *Pentavalent Uranium Oxide via Reduction of* [*UO*₂]²⁺ *Under Hydrothermal Reaction Conditions*, Inorg. Chem., 2008, 47 (21), pp. 10135-10140. *B DOI: 10.1021/ic801534m

EXAFS analysis



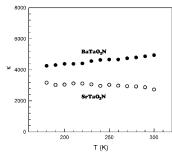
The crystal structure refined from the XRD is consistent with the EXAFS

How we understand EXAFS An example: FeS₂ (More examples

Dielectric materials (I)

Tantalum oxynitrides are a class of dielectric materials with high K which is tunable by selection of the A cation. By mixing A cations, a temperature-constant dielectric is possible.





First principles DFT on BaTaO₂N suggests that the different ionic radii of O and N introduce substantial disorder around the Ta atom.

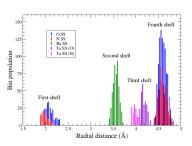
B. Ravel et al., Role of local disorder in the dielectric response of $BaTaO_2N$, Phys. Rev. B73, p. 184121 (2006),

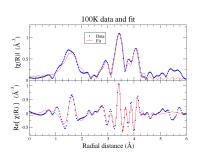
¹a DOI: 10.1103/PhysRevB.73.184121

How we understand EXAFS An example: FeS₂ More examples

Dielectric materials (II)

The DFT results in a rather complex coordination environment about the Ta atom — much more complex than the simple perovskite structure.





With some effort, this complexity can be incorporated into the data analysis. The EXAFS data are shown to be (mostly) consistent with the DFT results.

B. Ravel et al., Role of local disorder in the dielectric response of $BaTaO_2N$, Phys. Rev. B73, p. 184121 (2006),

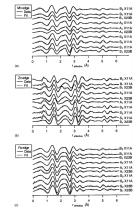
¹a DOI: 10.1103/PhysRevB.73.184121

How we understand EXAFS An example: FeS₂ (More examples)

EXAFS analysis can be quite elaborate...



Oxygen Octahedral site Tetrahedral



- Manganese zinc ferrite nanoparticles
- Each element can occupy each either metal site
- Oxygen vacancies can exist
- Data collected at 3 edges and on various sample preparations
- A fitting model was created using all the data simultaneously and considering occupancies of each metal on each site, oxygen vacancy, and nanoparticle undercoordination

S. Calvin et el., Multiedge refinement of extended x-ray-absorption fine structure of manganese zinc ferrite nanoparticles, Phys. Rev. B 66(22) p. 224405. (2002), a DOI: 10.1103/PhysRevB.66.224405 Ferrite image from a http://wikis.ilb.n.csu.edu/nhdex.php/Tmage:sisze21.png

A real world example More information

Part 4

A real-world example

My vegetable garden

When I bought my house, there was a wooden deck off the dining room. I replaced this with a paving stone patio and converted the adjacent plot of ground into a vegetable garden.





Wood preservative

The wood used to make the deck was treated with the wood preservative chromated copper arsentate (CCA), which is chromium-bearing analogue of copper orthoarsente, $Cu_3(AsO_4)_2 \cdot 4H_2O$.

$$(Cu^{2+})_3 \begin{bmatrix} O \\ II \\ -O & O^- \end{bmatrix}_2$$

CCA-treated wood is known to leach all three elements into surrounding soils. I had some questions:

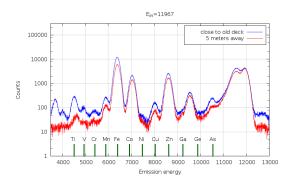
- Mow much As is in the soil? Is it higher near the patio than elsewhere in the garden? (Use XRF)
- What chemical species is the As in the soil? (Use XAS)

XRF spectra

I took soil samples from a few centimeters below the surface from a spot adjecent to the old deck and from a spot 5 meters away and slightly uphill.



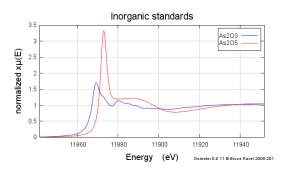
Here are the XRF spectra from those two spots:



There is a clear enhancement of both As and Cr in the soil adjacent to the old deck. The As is enhanced roughly two-fold.

As standards

As a point of reference, here are the XAS spectra from two inorganic As standards, $As_2^{3+}O_3$ and $As_2^{5+}O_5$.

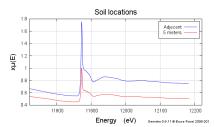


Note that the edge of As⁵⁺ standard is shifted substantially to higher energy and that the first peak is much enhanced.

As $^{5+}$ is water soluble, thus more mobile than As $^{3+}$. Also As $^{5+}$ is quite toxic.

XAS from the soil samples

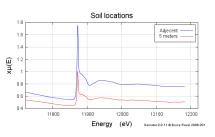
Here are the raw $\mu(E)$ data from the two soil locations. Sure enough, the signal from the site adjacent to the old deck is enhanced by about a factor of 2.



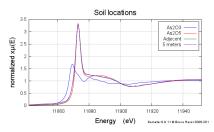
Should I be worried about eating produce from my garden?

XAS from the soil samples

Here are the raw $\mu(E)$ data from the two soil locations. Sure enough, the signal from the site adjacent to the old deck is enhanced by about a factor of 2.



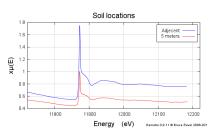
Here are the normalized data compared to standards. The As is slightly reduced, but predominantly As⁵⁺. As in soil is well known to bind to soil particles as As⁵⁺.



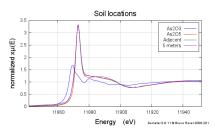
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XAS from the soil samples

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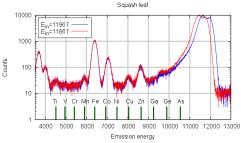
Here are the normalized data compared to standards. The As is slightly reduced, but predominantly As⁵⁺. As in soil is well known to bind to soil particles as As⁵⁺.



Should I be worried about eating produce from my garden?

XRF spectra from plant leaves

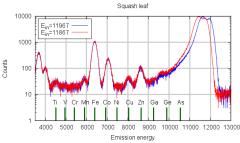
Here are XRF spectra from the leaf of a squash plant growing in the soil adjacent to the old deck.



Although toxic As⁵⁺ is present in the soil in elevated quantities, very little is taken up by the plants growing that soil.

XRF spectra from plant leaves

Here are XRF spectra from the leaf of a squash plant growing in the soil adjacent to the old deck.



Although toxic As⁵⁺ is present in the soil in elevated quantities, very little is taken up by the plants growing that soil.



The squash were delicious!

More information

About NSLS-II

http://www.bnl.gov/nsls2

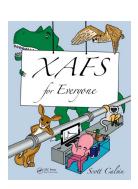
About synchrotron science

http://www.lightsources.org/

About X-ray Absorption Spectroscopy

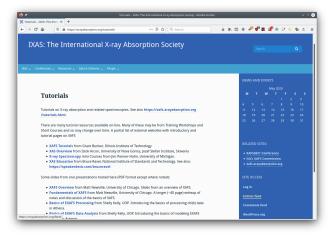
http://www.xrayabsorption.org/

XAFS for Everyone by Scott Calvin



Information about XAS

http://xrayabsorption.org/Tutorials



Free* XAS software

http://bruceravel.github.io/demeter/

